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Supplementary Examination (For Even Semester)-2023

Paper Name: Mathematical Foundations For Computer Applications

Paper Code: MCA-201

Time: 3 Hours

Maximum Marks: 75

Note: Programmable calculator is not allowed.

PART -A

(All questions are compulsory)

4X 5 = 20

S. No	Questions	Marks	Course Outcomes	Blooms Taxonomy Level																		
Q.1	Construct the distribution function and compute $P(X > \frac{1}{2})$, where $f(x) = \begin{cases} cx & \text{if } 1 > x > 0 \\ 0 & \text{otherwise} \end{cases}$ is a probability density function, for some constant c .	5	CO3	L6																		
Q.2	Find the rank of a matrix A , where $A = \begin{bmatrix} 1 & 2 & 0 & -1 \\ 3 & 4 & 1 & 2 \\ -2 & 3 & 2 & 5 \end{bmatrix}$.	5	CO2	L3																		
Q.3	A new couple, known to have two children, has just moved into town. Suppose that the mother is encountered walking with one of her children. If this child is a girl, what is the probability that both children are girls?	5	CO3	L4																		
Q.4	Estimate mean, mode, median, first quartile and third quartile from the following distribution of marks obtained by forty-nine students in the Mathematics class. <table border="1"> <tr> <td>X</td> <td>0-5</td> <td>5-10</td> <td>10-15</td> <td>15-20</td> <td>20-25</td> <td>25-30</td> <td>30-35</td> <td>35-40</td> </tr> <tr> <td>f(x)</td> <td>2</td> <td>4</td> <td>6</td> <td>15</td> <td>10</td> <td>5</td> <td>4</td> <td>3</td> </tr> </table>	X	0-5	5-10	10-15	15-20	20-25	25-30	30-35	35-40	f(x)	2	4	6	15	10	5	4	3	5	CO4	L4
X	0-5	5-10	10-15	15-20	20-25	25-30	30-35	35-40														
f(x)	2	4	6	15	10	5	4	3														
Q.5	Define equivalence relation. Let a relation R on the set of real numbers be defined as <i>if and only if</i> $1 + ab > 0$. Prove that R is symmetric and reflexive but not transitive.	5	CO1	L3																		

Q.6	Find the characteristic equation of the matrix $A = \begin{bmatrix} 5 & 7 \\ 3 & 4 \end{bmatrix}$.	5	CO2	L3
Q.7	Define the following terms with example: (a) Complete graph (b) Planar graph (c) Out-degree in directed graph (d) In-degree in directed graph (e) Regular graph.	5	CO5	L2

PART – B

(Attempt any Four Questions out of Six)

(4 X 10 = 40)

S. No	Questions	Marks	Course Outcomes	Blooms Taxonomy Level																		
Q.1	Investigate the values of θ & φ so that the equations $x+y+z=10$, $2x + y - 2z=7$, $x+y+\theta z=\varphi$ have (i) no solution (ii) a unique solution.	10	CO2	L5																		
Q.2	Explain the following terms with example: (i) Bipartite graph (ii) Eulerian path (iii) Eulerian circuit (iv) Complete bipartite graph (v) Weighted graph. Also explain handshaking theorem.	10	CO5	L2																		
Q.3	A random variable X has the following distribution <table><tr><td>x</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td></tr><tr><td>$f(x)$</td><td>K</td><td>2k</td><td>3k</td><td>4k</td><td>5k</td><td>6k</td><td>7k</td><td>8k</td></tr></table> Determine (i) k (ii) the probability distribution function (ii) $E(x)$ (iii) $E(x^2)$ (iv) variance (v) $P(2 \leq x \leq 5)$.	x	1	2	3	4	5	6	7	8	$f(x)$	K	2k	3k	4k	5k	6k	7k	8k	10	CO3	L4
x	1	2	3	4	5	6	7	8														
$f(x)$	K	2k	3k	4k	5k	6k	7k	8k														
Q.4	In a bolt machines A, B and C produces 25%, 35% and 40% respectively of the total product. Of their output, 5%, 4% and 2% are defective bolts. A bolt is chosen at random from the product and found to be defective. What are the probabilities that the bolt was produced either by machine A or by machine B or by machine C?	10	CO3	L4																		
Q.5	Solve the difference equation $a_r + a_{r-1} + 6a_{r-2} = r^2$, $a_0 = 1$, $a_1 = 2$.	10	CO1	L3																		
Q.6	Fit the straight line $Y = p + qX$ for the following data: <table><tr><td>X</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td></tr><tr><td>Y</td><td>1</td><td>5</td><td>10</td><td>22</td><td>38</td></tr></table>	X	0	1	2	3	4	Y	1	5	10	22	38	10	CO4	L5						
X	0	1	2	3	4																	
Y	1	5	10	22	38																	

BL – Bloom's Taxonomy Levels (1- Remembering, 2- Understanding, 3- Applying, 4- Analyzing, 5- Evaluating, 6- Creating)

CO-Course Outcomes

*****End of Paper*****